

7.63

$$u = \frac{1}{\sqrt{x^2 + y^2 + z^2}}, \quad u = (x^2 + y^2 + z^2)^{-1/2}$$

$$u'_x = \frac{-x}{\sqrt{(x^2 + y^2 + z^2)^3}}, \quad u''_{xy} = \left( -\frac{x}{\sqrt{(x^2 + y^2 + z^2)^3}} \right)'_y = \frac{3xy}{(x^2 + y^2 + z^2)^{5/2}}$$

$$u'_y = -\frac{y}{\sqrt{(x^2 + y^2 + z^2)^3}}, \quad u''_{xx} = \frac{2x^2 - y^2 - z^2}{(x^2 + y^2 + z^2)^{5/2}}$$

$$u'_z = -\frac{z}{\sqrt{(x^2 + y^2 + z^2)^3}}$$

$$1198 \quad r = \rho^2 \sin^4 \theta, \quad \frac{\partial r}{\partial \rho} = ? \quad \frac{\partial r}{\partial \theta} = ?$$

$$\frac{\partial r}{\partial \rho} = 2\rho \sin^4 \theta, \quad \frac{\partial r}{\partial \theta} = 4\rho^2 \sin^3 \theta \cos \theta$$

$$1200 \quad z = e^{xy(x^2 + y^2)}$$

$$\frac{\partial z}{\partial x} = e^{xy(x^2 + y^2)} (y(x^2 + y^2) + xy \cdot 2x) = (3x^2 y + y^3) e^{xy(x^2 + y^2)}$$

$$\frac{\partial z}{\partial y} = e^{xy(x^2 + y^2)} (x(x^2 + y^2) + xy \cdot 2y) = (3xy^2 + x^3) e^{xy(x^2 + y^2)}$$

$$1202 \quad u = e^{\frac{x}{y}} + e^{-\frac{z}{y}}$$

$$u'_x = e^{\frac{x}{y}} \cdot \frac{1}{y} = \frac{e^{x/y}}{y}; \quad u'_y = \frac{x e^{x/y}}{y^2} + \frac{z e^{-z/y}}{y^2}$$

$$u'_z = -\frac{1}{y} e^{-z/y}$$