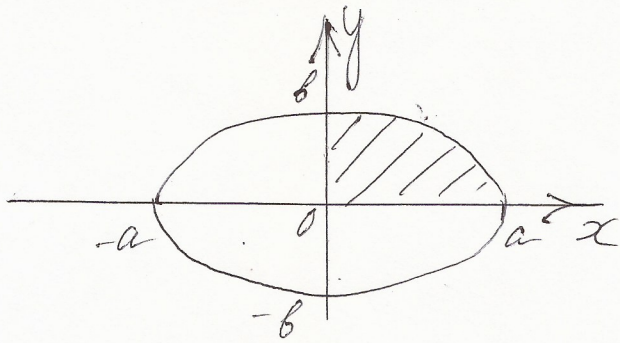


3) Найдем площадь области, ограниченной
 хордой, опирающейся на эллипс $\begin{cases} x = acost, \\ y = bsint. \end{cases}$



$$S = \int_{t_1}^{t_2} y(t) x'_t dt$$

$$\begin{cases} x(t) = acost, \\ y(t) = bsint \end{cases}$$

$$dx = -asint dt$$

$$\frac{1}{4} S: 0 \leq x \leq a$$

$$\begin{matrix} (0; b) & \longrightarrow & (a; 0) \\ t_1 & & t_2 \end{matrix}$$

$$t_1: \begin{cases} 0 = acost_1, \\ b = bsint_1, \end{cases} \Rightarrow \begin{cases} cost_1 = 0 \\ sint_1 = 1 \end{cases} \Rightarrow t_1 = \frac{\pi}{2}$$

$$t_2: \begin{cases} a = acost_2, \\ 0 = bsint_2, \end{cases} \Rightarrow \begin{cases} cost_2 = 1 \\ sint_2 = 0 \end{cases} \Rightarrow t_2 = 0$$

$$S = 4 \int_{\frac{\pi}{2}}^0 bsint \cdot (-asint) dt = -4ab \int_{\frac{\pi}{2}}^0 \sin^2 t dt =$$

$$= 4ab \int_0^{\frac{\pi}{2}} \frac{1 - \cos 2t}{2} dt = \frac{4ab}{2} \left(\int_0^{\frac{\pi}{2}} dt - \frac{1}{2} \int_0^{\frac{\pi}{2}} \cos 2t d(2t) \right) =$$

$$= 2ab \left(t \Big|_0^{\frac{\pi}{2}} - \frac{1}{2} \sin 2t \Big|_0^{\frac{\pi}{2}} \right) = 2ab \left(\frac{\pi}{2} - 0 - \frac{1}{2} (\sin \frac{2\pi}{2} - \sin 0) \right) =$$

$$= 2ab \left(\frac{\pi}{2} - 0 - \frac{1}{2} \cdot 0 \right) = 2ab \cdot \frac{\pi}{2} = \pi ab$$

Площадь: $S = \pi ab$.